

Savitribai Phule Pune University
Hutatama Rajguru Mahavidyalaya, Rajgurunagar
F.Y.B.Sc.
MT-122: Calculus II
(2019 Pattern) (Semester-II) (Paper-II) (12112)

Time: 2 Hours

Max. Marks: 35

Instructions to the candidates:

- 1) All questions are compulsory.
- 2) Figures to the right indicate full marks.

Q1) Attempt any five of the following: [5]

- a) Show that every differential function is continuous.
- b) State Cauchy's mean value theorem.
- c) Define relative extremum function.
- d) Find general solution of homogeneous differential equation $y' + 3x^2y = 0$.
- e) Check whether following differential equation is exact or not
$$3x^2y^2 dx + 6x^3y dy = 0.$$
- f) Find n^{th} derivative of the function $y = a^{3x}, a > 0$.
- g) Evaluate $\lim_{x \rightarrow 0} \frac{e^x - 1 - x}{x^2}$.

Q2) A) Attempt any one of the following [5]

- a) State and prove Rolle's theorem.
- b) Find n^{th} derivative of $\cos^4 x$.

B) Attempt any one of the following [5]

- a) The function $f: \mathbb{R} \rightarrow \mathbb{R}$ defined by

$$f(x) = \begin{cases} x^2, & \text{if } x \geq 0 \\ -x^2, & \text{if } x < 0 \end{cases} \quad \text{show that } f \text{ is differential at } x = 0.$$

- b) Using Taylor series expansion find the approximate value of $\sqrt{25.15}$.

Q3) A) Attempt any one of the following [5]

- a) If $P(x)$ is continuous on (a,b) then the general solution of the homogeneous equation $\frac{dy}{dx} + P(x)y = 0$ on (a,b) is $y = ce^{-\phi(x)}$ where

$$\phi(x) = \int P(x)dx, \quad a < x < b.$$

- b) Find integrating factor for

$$(5xy + 2y + 5)dx + (2x)dy = 0.$$

B) Attempt any one of the following [5]

- a) Evaluate $\lim_{x \rightarrow 0} \frac{1}{x} - \frac{1}{\sin x}$.

- b) Verify the Lagrange's mean value theorem for the function $f(x) = \sqrt{x}$ on $[1,9]$.

Q4) A) Attempt any one of the following [5]

- a) Explain method of variation of parameter.
- b) Define exact differential equation. Explain the method of solving exact differential equation.

B) Attempt any one of the following [5]

- a) Solve the Bernoulli's equation $y' + y = y^2$.
- b) Find the general solution of following differential equation by method of variation of parameter $y' + (\tan x) y = \cos x$.